

UDC 330.341=111

DOI: 10.5862/JE.216.16

S.A. Bakanova, G.Iu. Silkina

KNOWLEDGE DISSEMINATION PROCESS IN PARAMETRIZED NETWORKS OF ENTERPRISES

С.А. Баканова, Г.Ю. Силкина

ПРОЦЕССЫ РАСПРОСТРАНЕНИЯ ЗНАНИЙ В ПАРАМЕТРИЗОВАННОЙ СЕТИ ИНФОРМАЦИОННЫХ ОБМЕНОВ

The article contains a mathematical model of parametrized network of knowledge exchange. It considers a process of knowledge spreading among a group of people united by common professional interests (a company or its sub-unit). A network is described by a fuzzy graph where vertices stand for individuals and edges – for contacts between them. A fuzzy set of edges defines the process quality characteristics that have direct influence on the result: coincidence of professional interests of individuals (in the model - cognitive potential of knowledge transfer) and evaluation of communication activity between them (how often they communicate – communication intensity). The first parameter is defined on the base of knowledge structure of individuals (for particular knowledge domain). The second one communication intensity - is counted on information of communication occurrence (one-on-one communication, in groups, round tables and other ways of communication are taken into account). On the base of the quality parameters of relation between members of a group the model define clusters in a network (connected components in the graph theory) - subgroups of individuals that have strong productive communication among them. The model has a set of overall process characteristics of the process of knowledge spreading and may be used for analysis of network states in different timestamps and as consequence of all that – for knowledge management support. Information for analysis can be retrieved for corporate social networks. The model itself and its instruments can be added as an add-on to corporate networks to sustain knowledge management in organization. The article contains an example of the model use (calculation, analysis, illustration of fuzzy graphs). It defines the model's advantages and probable ways of improvement. KNOWLEDGE SPREADING; ORGANIZATIONS; MODEL OF KNOWLEDGE SPREADING; GRAPH; CHARACTERISTICS OF KNOWLEDGE SPREADING PROCESS; CORPORATE SOCIAL NETWORKS.

В статье представлена разработанная авторами модель параметризованной сети информационных обменов. Рассматривается процесс распространения знаний внутри группы людей, объединенных профессиональными интересами (организации различных форм собственности, их структурные подразделения). Сеть описывается нечетким неориентированным графом первого рода, в котором вершины идентифицируют индивидов, а ребра – связи между ними. Нечеткое множество ребер графа задает качественные характеристики процесса распространения знаний, которые оказывают непосредственное влияние на результат рассматриваемого процесса: общность профессиональных интересов индивидов (когнитивный потенциал обмена знаниями) и оценка интенсивности их общения (как часто индивиды контактируют). Первый показатель строится на основе данных о структуре знаний индивидов в определенной области профессиональных знаний. Показатель интенсивности взаимодействия сотрудников определяется на основе информации о частоте их общения (общение один на один, общение в группах, на семинарах, круглых столах и т. д.). На основе введенных показателей качества связи между индивидами в сети выделяются кластеры (в теории графов - компоненты связности) — подгруппы индивидов, между которыми происходит особенно интенсивное общение. Модель включает набор обобщающих характеристик процессов распространения знаний, которые могут быть использованы для анализа текущего состояния сети. Информация, необходимая для вычислений может быть извлечена из корпоративных социальных сетей, поддерживающих организацию и хранение профилей сотрудников (их знаний и компетенций), электронные средства коммуникации и базы корпоративных знаний. Сам разработанный модельный инструментарий может быть добавлен в качестве надстройки в корпоративную социальную сеть для сравнительного анализа и поддержки управленческих решений в сфере менеджмента знаний. Работа модели иллюстрируется расчетным примером (приведены результаты расчетов, их анализ и иллюстрации нечетких графов). Определены достоинства модели и направления ее доработки.

РАСПРОСТРАНЕНИЕ ЗНАНИЙ; ОРГАНИЗАЦИИ; МОДЕЛЬ РАСПРОСТРАНЕНИЯ ЗНАНИЙ; ГРАФ; ХА-РАКТЕРИСТИКИ РАСПРОСТРАНЕНИЯ ЗНАНИЙ; КОРПОРАТИВНАЯ СОЦИАЬНАЯ СЕТЬ.

Introduction. In the modern world investment in human capital, on the one hand, and the development of infrastructure for knowledge exchange, on the other hand, determine possibility of process of employees innovation creativity and, as a result, a company's success in market. Validity of this assertion, set out in the report «The Global Innovation Index 2014», has been proved theoretically and repeatedly reaffirmed with real business practices [1]. Thereby, applied research in the area of knowledge management in enterprises becomes a subject of top interest. An increased number of domestic and foreign scientific and practical essays shows the value of this trend [2].

In a broad sense, knowledge management implies the process of creation, accumulation and distribution of it among people [3]. All the components of this process are fundamentally important for the success of modern companies, but are significantly different from the viewpoint of possibility of scientific formalization, justification and implementation of particular management decisions. In this sense, a creative process of knowledge production is the most difficult part; the problem of knowledge accumulation can be easily solved considering the current level of information technologies. And, finally, the knowledge dissemination, which involves not only using of modern communication tools, but, mainly, the interaction of knowledge carriers is, in the authors' opinion, the cornerstone of the knowledge management process and is of the greatest scientific interest for them.

The basic form of distribution of «working» knowledge (mainly, implicit) at all times have been an exchange of knowledge through the direct communication between people. Today, all the geographical, time and bureaucratic communication barriers and, consequently, knowledge sharing barriers are almost faded [4]. And this positive fact is one of the reasons for the increased involvement of employees of advanced technology industries, scientific and research organizations in the global knowledge exchange process. As a consequence, the interest of business and science communities for tools of analysis and optimization of processes occurring during this exchange greatly increased.

The existence and practical significance of a number of qualitative conditions of the productive knowledge exchange is a difficulty for formalization and simultaneously a great challenge to academic community. At the stage of searching for different approaches to the description of this process the authors can not ignore the various properties of knowledge (knowledge can be explicit or implicit, knowledge is inexhaustible in its essence), exchange participants (each person has their own set of knowledge) and forms of the process (direct communication, attending conferences, participation in roundtables, etc.) [5].

of the existing scientific Analysis and methodological initiatives. The models presented in [6-8] can be distinguished as knowledge dissemination models. The selected models aim to justify and formalize the key factor in knowledge dissemination - cognitive distance between employees («remoteness» of individuals in knowledge aspect). However, these models have shortcomings, such as static character, lack of analytical justification and sufficient assessment of the qualitative aspects of the process. Simultaneously, these shortcomings determine the direction of their improvement.

Another group of models [9], used to represent knowledge exchange processes in organizations, is based on the mathematical tools for description and analysis of communication networks. In the models it simulates the space and time aspects of information exchange between the participants of social networks, which imposes certain limitations on possibility of using it for the formalization and analysis of knowledge exchange.

The endeavor to make a positive contribution to the critical remarks and to present own vision of knowledge distribution processes was the initial motive of writing this article. Moreover the existing mathematical apparatus provides opportunities to achieve the goal.

Commonality which unites the above mentioned models is that they are based on the ideology of graph theory, which is the most appropriate tool to reflect the relations between objects. In terms of this theory, objects are represented as graph with vertices $v_i \in V$, and relations (links) between them either undirected edges $e_i \in E$ or directed arcs of the graph $a_i \in A$; graph in general – a tuple $G = \langle V, E \rangle$ or $D = \langle V, A \rangle.$ Herewith, the nature and characteristics of the relations between objects in no way is taken into account: it is only important that the connection exists, and information about it is available.

In due time the development of classical graph theory was determined by networks – weighted graphs, which edges and arcs were credited with numerical parameters quantitatively characterizing the existing links: distance, time, cost, etc. On this basis there were created and developed networking models of process, which are now widely used in transport planning, organization of project work, etc.

A key and at the same time a non-numerical nature aspects for knowledge exchange process are the characteristics of relations between people – the intensity of subject communication and matching of degree of professional interests (knowledge) in a particular area, defining the very possibility of knowledge exchange. For a quantitative image of these characteristics, we suggest to use apparatus of fuzzy graphs.

For development of the classic graphs theory positions the tuple $\tilde{G} = \langle V, \tilde{E} \rangle$ is called as fuzzy undirected graph of the first kind, where V – conventional (clear) set of vertices, $\tilde{E} = \langle \mu_E(v_i, v_i) / \{v_i, v_i\} \rangle$ – fuzzy set of edges, where $v_i, v_j \in V, \mu_E : E \to [0, 1]$ – membership function, $\mu_E(v_i, v_i)$ – membership function value for the edge $\{v_i, v_j\}$, which characterize in one sense or another «quality» of connection between vertices v_i μ v_i . There are no other formal imposed restrictions on μ , so any function defined on the set of edges and taking values from the segment [0, 1] can be interpreted as the membership function [10].

The results of the implementation of the announced approach to modeling the propagation of knowledge are presented in this article.

Parameterization of networks of knowledge exchange. Let us consider a process of knowledge exchange among people united by professional interests (enterprises and their subdivisions). This process is defined by time and space measures. Employees and professional contacts between them represent a network of knowledge dissemination.

The network is modeled by a fuzzy graph: $\tilde{G} = \langle V, \tilde{E} \rangle$ — is a set of vertices that identify employees and \tilde{E} — is a fuzzy set of edges that describes professional contacts between employees ($E = \{e_{ij}\}$ — is a fuzzy set carrier each element defines whether a professional communication between two people takes place).

As a membership function for the fuzzy set of the graph edges the model considers two parameters that define the possibility and the result of knowledge dissemination process – density of communication between employees and cognitive potential of knowledge exchange.

The cognitive potential of knowledge sharing between two individuals defines to which extent their professional knowledge coincide. It is assumed that the exchange of knowledge between two employees is possible when the participants can easily speak the same «professional language» and can communicate on the same topic.

As it is shown in [7] graph vertices are determined by not just labels, but by a set of knowledge elements, formally expressed as a vector $v_i = (((x_k)_l)_m)$ where x - is a component of a certain field of knowledge and takes value of 0 or 1 depending on whether an employee has this knowledge or not, m = 1, 2, ..., M - subject groups of knowledge, $l_m = 1, ..., L_m -$ fields of knowledge, $k_{lm} = 1, ..., K_{ml} -$ components (elements) of knowledge.

Vector form of employee knowledge allows evaluating of cognitive potential for knowledge sharing between the two employees, numerically determining the «angle» between the vectors (disparity direction) of their knowledge.

Formally, the cognitive potential of knowledge sharing on the certain field of knowledge between the two network agents (employees) i and j we offer to calculate using the formula:

$$\alpha_{ij}^{l_m} = \frac{(v_i \cdot v_j)^{l_m}}{|v_i|^{l_m} \cdot |v_j|^{l_m}} = \frac{\sum_{k=1}^K x_k y_k}{\sqrt{\sum_{k=1}^K (x_k)^2} \cdot \sqrt{\sum_{k=1}^K (y_k)^2}}, \quad (1)$$

where $v_i = (((x_k)_l)_m)$ and $v_j = (((y_k)_l)_m)$ – knowledge vectors of employees with indexes *i* and *j*.

Here in the numerator – the amount of paired products of the coordinates (scalar product) and in the denominator – the product of the lengths of these vectors.

The reasons for the proposed approach are the following. In low-dimensional spaces, where the vector is directed segments, a similar formula calculates the cosine of the angle between the vectors. At full coincidence directions vectors cosine of the angle between them equals 1; divergence of directions reduces it down to a value of 0 (orthogonal vectors). Extrapolation of this approach in a higher dimensional space allows meaningful interpretation of $\alpha_{ij}^{l_m}$ as an indicator of the degree of closeness of knowledge of employees. The fact that the parameter takes values in the interval [0; 1] allows using it as a membership function in the fuzzy set determining the edges of the graph:

 $\tilde{E} = \left\langle \alpha_{ij}(v_i, v_j) / \{v_i, v_j\} \right\rangle.$

The second characteristic of the process of knowledge dissemination in the model is the intensity of communication which formally can be measured by the number of acts of communication for a certain time period. When describing the diffusion of knowledge it is reasonable not to limit it to only formal communication (trainings, round tables, etc.), but also include consideration of informal communication - as one of the key distribution channels of «working» tacit knowledge. As long as we are not limited by a form of knowledge transfer and talk about the impact of this of communication in terms knowledge dissemination, quantitative at first glance characteristic (how many times two employees talked) turns into qualitative one.

Given the latter, the authors propose to evaluate the relationship between the employees in terms of it to be «full-fledged» assuming that if the contact between individuals «full-fledged» the transfer of knowledge is considered to be working. Otherwise, communication between employees is considered partial.

In the model, this premise is expressed as follows:

Let $\delta_{ij} = \frac{t_{ij}}{T}$ be the amount of communication

over a communication channel between employees with indexes *i* and *j* (number of acts of intercourse between individuals over the time period, T – the length of the time period in days) and $\overline{\delta} = \frac{1}{|E|} \sum_{i,j: \{v_i, v_j\} \in V} \delta_{ij}$ – average number

of pairs of communication between employees in the network.

Then the characteristic of communication intensity between individuals is defined as follows:

$$\beta(e_{ij}) = \begin{cases} 1, & \delta_{ij} \ge \overline{\delta}, \\ \delta_{ij} / \overline{\delta}, & \delta_{ij} < \overline{\delta}. \end{cases}$$
(2)

The parameter $\beta(e_{ij})$ also takes values in the interval [0; 1], which allows us to interpret it as a membership function for the fuzzy defining of the edges of the graph: $\tilde{E} = \langle \beta_{ij}(v_i, v_j) / \{v_i, v_j\} \rangle$.

Dissemination of knowledge in the parameterized network. To describe the process of knowledge dissemination in professional networks the model uses the concept of parameterized routes. A route in a graph is determined by a set of alternating edges and vertices in which any two adjacent elements incident. Routes can be interpreted as ways in which knowledge disseminates from its original owner to probable recipients.

Based on figures parametrizing knowledge networks (the cognitive potential and the communication intensity), the model identifies the characteristics of routes that have their own meaningful interpretation.

The theory of fuzzy graphs uses various characteristics of routes between nodes and each of them can be interpreted in terms of knowledge propagation process. The model presented in this paper uses three kinds of routes strength – conjunctive, disjunctive and cumulative. Conjunctive and disjunctive strength define edges with the lowest or highest cognitive potentials, (in cognitive respectively units). These characteristics can be used to analyze the strength of the range of the route, to identify strong and weak links in the path.

For a route $L(v_i, v_j)$ connecting vertices with numbers *i* and *j* conjunctive and disjunctive strength accordingly in the model defined as follows (examples of calculation formulas for cognitive units):

$$\eta^{\alpha}_{\&}(L(v_i, v_j)) = \underset{\langle v_e, v_m \rangle \in L(v_i, v_j)}{\&} \alpha \langle v_e, v_m \rangle, \quad (3)$$

$$\eta^{\alpha}_{\vee}(L(v_i, v_j)) = \bigvee_{\langle v_e, v_m \rangle \in L(v_i, v_j)} \alpha \langle v_e, v_m \rangle.$$
(4)

The cumulative strength of the route (in terms of cognitive and time units) characterizes the entire route as a whole, its overall «reliability» to transfer knowledge from one to another vertex. A need for such index occurs when a comparative characteristic of various knowledge flow directions from the initiator are required, as well as for construction of complex propagation characteristics in the knowledge network. Formally, the cumulative strength of the route is defined as follows:

$$\eta_{\times}^{\alpha}(L(v_i, v_j)) = \underset{\langle v_e, v_m \rangle \in L(v_i, v_j)}{\times} \alpha \langle v_e, v_m \rangle.$$
(5)

In professional networks the cumulative maximum strength of the route can be interpreted as the most reliable direction of knowledge dissemination.

The parameter of maximum cumulative strength in the model is shown by a fuzzy reachability matrix of vertices (analog of reachability matrix in the classic graph theory), in which each element shows the most «strong» («reliable») route between the vertices.

Technically fuzzy reachability matrix is constructed in several stages as follows.

1. We construct a fuzzy adjacency matrix by the parameters of cognitive potential of knowledge for all pairs of vertices with specified level of intensity of their communication (λ^{β}) :

 $\tilde{S}_{\alpha} = \left(\alpha_{ij} \mid \beta_{ij} \geq \lambda^{\beta} \right).$

By their meaning, elements of these matrices correspond to paths of length 1 in the parameterized network. Routes of greater lengths represented by corresponding degrees of adjacency matrix.

2. The model uses the following rule of matrix multiplication.

Each element of the result matrix is the maximum of element-wise product of a line to a column that is different from zero, if the number of the element in the line does not match the item in the column:

$$\begin{split} \tilde{S}_{\alpha} \cdot \tilde{S}_{\alpha} &= \tilde{S}_{\alpha}^{2} = C; \\ c_{ij} &= \begin{bmatrix} \max\left\{\alpha_{ir} \cdot \alpha_{rj}\right\}, \ r = 1, \dots, n, \ i \neq j, \\ 0, \qquad i = j. \end{split}$$

Fuzzy adjacency matrix raised to the powers from 2 to n - 1. Each of the resulting matrix contains in fact the strongest possible routes of length k between two vertices: \tilde{S}_{a}^{2} , \tilde{S}_{a}^{3} , ..., \tilde{S}_{a}^{n-1} .

3. Final fuzzy reachability matrix by is defined element-wise comparison of matrices $\tilde{S}_{\alpha}, \tilde{S}_{\alpha}^2, \tilde{S}_{\alpha}^3, \dots, \tilde{S}_{\alpha}^{n-1}$:

$$d_{ij}^{\alpha} = \max\left\{\alpha_{ij}^{k}\right\}, k = 2, \dots, n-1.$$

The resulting matrix contains elements that characterize the maximum strength of the path between two vertices in the graph in cognitive terms, taking into account the necessary intensity of communication between individuals.

Clustering of parameterized knowledge dissemination network. Characteristic feature of all communities (professional or interest) is the allocation of small subgroups in which there is the most intensive communication between their members. Companies and their subdivisions are not exception to this rule [11].

Theory of Graphs provides tools for searching connection components — sets of employees «united» with the same interests — vertices of a graph based on the relations between them. In the case of «simple» not parameterized network (as shown in [7]), the connection components will substantively mean disjoint classes with no connection in-between that is knowledge exchange is impossible. Network without any parameters allows only roughly estimate its internal division into isolated subgroups, limiting the ability of full analysis of its structure due to the fact that the factors of communication intensity and proximity of professional interests are not included.

Parameterized network based on coincidence of interests and intensity of employees' communication, through selection of connection components is divided into clusters – cohesive groups of information exchange with an intensive productive communication within, but at the same time with the links to external vertices and groups. In contrast to classes (defined in the network with no parameters), division into clusters in the graph occurs within the parameters of individuals' communication and enables structural analysis, evaluation of interest groups network coverage.

Interest groups of parameterized network are determined by introducing of minimum admissible strength coefficient $-\lambda^{\alpha}$ (λ^{β}), that fixes required intensity of communication or cognitive capacity among the employees. Based on the fuzzy adjacency matrix of vertices and the minimum allowable bond strength index, it is determined in the model by a binary matrix of elements' connection $(T_{n\times n}^{\alpha})$, that is determinate analogue of fuzzy reachability matrix (for example, cognitive strength):

$$t_{ij}^{\alpha} = egin{bmatrix} 1, \ d_{ij}^{lpha} \geq \lambda^{lpha}, \ 0, \ d_{ij}^{lpha} \prec \lambda^{lpha}, \end{cases}$$

137

where λ^{α} – the minimum acceptable level of strength of the way between the vertices in cognitive units.

The final matrix $T_{n \times n}$ $(t_{ij} = t_{ij}^{\alpha} \cdot t_{ij}^{\beta})$ identifies substantively the «strong», «working» network links between agents considering cognitive potential and intensity of communication and it is interpreted by the authors as a connection matrix of an undirected graph vertices. According to the well-known in graph theory algorithm connection components are found on vertices connection matrix.

Parametrized network characteristics. Analysis and modeling of economic processes are focused on the development and justification of management decisions. The process of knowledge dissemination, covered in this article, and the suggested by the authors approach to its' analysis is not an exception in this respect. In this paper we offer a set of indicators by means of which it is possible to analyze knowledge dissemination networks and some practical recommendations for improving the conductivity of new knowledge in networks are given also.

Configuration network characteristics (characteristics of elements) and processes of knowledge distribution characteristics are defined in the model.

Characteristics of vertices in the parameterized network of knowledge dissemination. Each vertex in the graph (individual in a professional network) can be characterized in terms of cognitive and time «distance» from their nearest neighbors:

$$b_{\alpha}(v_i) = \overline{\alpha}_{ij} = \frac{\sum_{j} \alpha_{ij}}{\left| \Gamma(v_i) \right|}, \tag{7}$$

where $\Gamma(v_i)$ – the set of vertices reachable from v_i by a single step. The indicator shows the average cognitive «distance» of the individuals from their neighbors. The time analog of the parameter (average «distance» in time units) is

calculated by:
$$b_{\beta}(v_i) = \overline{\beta}_{ij} = \frac{\sum_{j} \beta_{ij}}{|\Gamma(v_i)|}.$$

The indicators can help to assess every employee involved in the process of knowledge sharing. Overall analysis of the individuals using time and cognitive «distance» parameters will identify active participants in the exchange of knowledge among the others and that need to be motivated to get new knowledge and spread it on in the community (they can be sent to conferences, trainings etc).

Characteristics of knowledge dissemination process. For each field of knowledge used in professional community (enterprise), the model suggests the following characteristics of the process of knowledge sharing that can be used to analyze the process itself and to identify its probable sore points in the terms of knowledge sharing:

1. Potential scale of knowledge dissemination – amount of employees that able to «absorb» new knowledge from a particular field:

$$w_{l_m}^* = \left\{ v_i \mid \left(x_{klm} \right)_{l_m} > 0 \right\}.$$
 (9)

2. Average strength of the route in terms of cognitive units:

$$\overline{w}_{l_m}^{\alpha} = \frac{\sum\limits_{i, j=1}^n d_{ij}^{\alpha}}{n^2}.$$
 (10)

3. Average strength of the route in terms of time units:

$$\bar{w}_{l_m}^{\beta} = \frac{\sum_{i, j=1}^n d_{ij}^{\beta}}{n^2}.$$
 (11)

4. The average number of interest groups (connected components):

$$\overline{V} = \frac{|V_p|}{p},\tag{12}$$

where $|V_p|$ – the amount of elements in the set.

Illustration of the model. Let us illustrate with a calculation example how the model works.

Suppose there is a group of 15 colleagues (employees of organization or department), associated with professional contacts and interests in the same area of expertise.

Fig. 1 shows a graph, illustrating the information exchange between the network members, where the edges are defined by the existence of contact between the vertices. Such network (and its model illustration) provides a first idea of how connections are established between individuals in the group.

There is the structure of the professional knowledge of each member of the group (Tab. 1) and the frequency of their communication (Tab. 2) per unit of time taken for one month. Professional knowledge of the area, which is used in a hypothetical group, divided into five components.



Fig. 1. Non-parameterized network of information exchanges in a team (vertices identify employees, edges – contacts between them on the principle of «individuals know each other personally»)

Table 1

The structure of the employees' knowledge

x_k v_i	v_1	<i>v</i> ₂	<i>v</i> ₃	v_4	v_5	<i>v</i> ₆	v_7	v_8	<i>v</i> 9	v_{10}	<i>v</i> ₁₁	<i>v</i> ₁₂	<i>v</i> ₁₃	<i>v</i> ₁₄	<i>v</i> ₁₅
x_1	1	0	0	0	1	1	1	0	1	1	1	0	1	0	0
x_2	1	1	0	0	1	1	0	0	1	1	1	0	1	0	1
x_3	0	1	0	1	1	1	0	0	1	1	1	0	1	1	1
x_4	1	1	1	0	0	1	0	0	1	0	1	0	1	0	0
x_5	0	1	0	0	1	1	0	1	1	0	1	1	1	1	1

Table 2

v_i	v_1	<i>v</i> ₂	<i>v</i> ₃	<i>v</i> ₄	<i>v</i> ₅	<i>v</i> ₆	v_7	v_8	<i>v</i> ₉	<i>v</i> ₁₀	<i>v</i> ₁₁	<i>v</i> ₁₂	<i>v</i> ₁₃	<i>v</i> ₁₄	<i>v</i> ₁₅
<i>v</i> ₁		1	0	0	0	0	0	0	0	2	0	0	0	0	0
v_2	1		0	0	6	4	0	0	0	3	0	0	0	0	0
<i>v</i> ₃	0	0		1	0	0	11	0	0	0	0	0	0	0	0
v_4	0	0	1		0	0	0	0	0	0	0	0	1	0	0
v_5	0	6	0	0		0	1	0	0	15	0	0	0	0	0
v_6	0	4	0	0	0		3	0	18	0	0	0	0	0	0
v_7	0	0	11	0	1	3		4	0	9	1	0	0	0	0
v_8	0	0	0	0	0	0	4		0	0	0	0	0	0	0
v_9	0	0	0	0	0	18	0	0		0	0	0	0	0	0
v_{10}	2	3	0	0	15	0	9	0	0		0	0	0	0	0
<i>v</i> ₁₁	0	0	0	0	0	0	1	0	0	0		0	0	1	0
<i>v</i> ₁₂	0	0	0	0	0	0	0	0	0	0	0		24	0	11
<i>v</i> ₁₃	0	0	0	1	0	0	0	0	0	0	0	24		0	0
<i>v</i> ₁₄	0	0	0	0	0	0	0	0	0	0	1	0	0		0
<i>v</i> ₁₅	0	0	0	0	0	0	0	0	0	0	0	11	0	0	

Amount of acts of communication between employees (t_{ij})

By the formulas (1) and (2) the network parameters are defined – the indicator of communication intensity and the cognitive potential of knowledge exchange between individuals. Tab. 3 shows the indicators for each pair of employees, and Fig. 2 illustrates a parameterized knowledge exchange network. The graph shown in Fig. 2 is an illustration the graph is painted in two colors – for the indicators of communication intensity and cognitive potential, respectively. For visualization of indicators we took gradation of colors, where the maximum intensity of the color corresponds to the highest value of indicator (each edge is marked with α and β symbols to designate correspondence between a component of the edge and its' index).

of the derived model calculations. Each edge of e

Table 3

	v_i													.,		
v_i	\backslash	v_1	<i>V</i> ₂	<i>V</i> ₃	<i>v</i> ₄	V_5	<i>v</i> ₆	<i>v</i> ₇	V_8	<i>V</i> 9	V_{10}	<i>v</i> ₁₁	<i>v</i> ₁₂	<i>V</i> ₁₃	<i>v</i> ₁₄	<i>v</i> ₁₅
v_1	α		0.6	0.6	0	0.6	0.8	0.6	0	0.8	0.7	0.8	0	0.8	0	0.3
	β		0.2	0	0	0	0	0	0	0	0.3	0	0	0	0	0
v_2	α	0.6		0.5	0.5	0.8	0.9	0	0.5	0.9	0.6	0.9	0.5	0.9	0.7	0.9
	β	0.2		0	0	0.9	0.6	0	0	0	0.5	0	0	0	0	0
<i>v</i> ₃	α	0.6	0.5		0	0	0.4	0	0	0.4	0	0.4	0	0.4	0	0
	β	0	0		0.2	0	0	1	0	0	0	0	0	0	0	0
v_4	α	0	0.5	0		0.5	0.4	0	0	0.4	0.6	0.4	0	0.4	0.7	0.6
	β	0	0	0.2		0	0	0	0	0	0	0	0	0.2	0	0
v_5	α	0.6	0.8	0	0.4		0.9	0.5	0.5	0.9	0.9	0.9	0.5	0.9	0.7	0.9
	β	0	0.9	0	0		0	0.2	0	0	1	0	0	0	0	0
v_6	α	0.8	0.9	0.4	0.4	0.9		0.4	0.4	1	0.8	1	0.4	1	0.6	0.8
	β	0	0.6	0	0	0		0.5	0	1	0	0	0	0	0	0
v_7	α	0.6	0	0	0	0.5	0.4		0	0.4	0.6	0.4	0	0.4	0	0
	β	0	0	1	0	0.2	0.5		0.6	0	1	0.2	0	0	0	0
v_8	α	0	0.5	0	0	0.5	0.4	0		0.4	0	0.4	1	0.4	0.7	0.6
	β	0	0	0	0	0	0	0.6		0	0	0	0	0	0	0
<i>v</i> ₉	α	0.8	0.9	0.4	0.4	0.9	1	0.4	0.4		0.8	1	0.4	1	0.6	0.8
	β	0	0	0	0	0	1	0	0		0	0	0	0	0	0
v_{10}	α	0.7	0.6	0	0.6	0.9	0.8	0.6	0	0.8		0.8	0	0.8	0.4	0.7
	β	0.3	0.5	0	0	1	0	1	0	0		0	0	0	0	0
<i>v</i> ₁₁	α	0.8	0.9	0.4	0.4	0.9	1	0.4	0.4	1	0.8		0.4	1	0.6	0.8
	β	0	0	0	0	0	0	0.2	0	0	0		0	0	0.2	0
<i>v</i> ₁₂	α	0	0.5	0	0	0.5	0.4	0	1	0.4	0	0.4		0.4	0.7	0.6
	β	0	0	0	0	0	0	0	0	0	0	0		1	0	1
<i>v</i> ₁₃	α	0.8	0.9	0.4	0.4	0.9	1	0.4	0.4	1	0.8	1	0.4		0.6	0.8
	β	0	0	0	0.2	0	0	0	0	0	0	0	1		0	0
<i>v</i> ₁₄	α	0	0.7	0	0.7	0.7	0.6	0	0.7	0.6	0.4	0.6	0.7	0.6		0.8
	β	0	0	0	0	0	0	0	0	0	0	0.2	0	0		0
<i>v</i> ₁₅	α	0.3	0.9	0	0.6	0.9	0.8	0	0.6	0.8	0.7	0.8	0.6	0.8	0.8	
	β	0	0	0	0	0	0	0	0	0	0	0	1	0	0	

Values of the communication intensity (β) and cognitive potential (α) for the network (each cell contains both ratings, the highlighted cells identify edges of the graph)



Fig. 2. Parameterized network of knowledge exchanges

Using the parameters of knowledge exchange in networks we can define routes and their characteristics that provide a value of each route and can be used to define conductivity properties of the network.

The presented approach to illustration of a parameterized network enables the primary analysis of the links in the network. Thus, for example, the edge between the vertices with the numbers 3 and 4 shows a very weak link for transfer of knowledge between the employees, in both cognitive and time units. In fact, this means that individuals do not have common interests and, moreover, communicate extremely seldom. In the model calculations parameters of the edge «3 - 4» are interpreted as conjunctive strength of routes passing through this edge. At the same time, exactly through this element knowledge exchange between a group of vertices with the numbers 12, 13, 15 and the rest of the members of the team is possible that makes this connection essentially important in terms of the conduction. The whole network most appropriate management decisions in this situation will be a redefinition of relations

between these two groups of employees (on one and on the other «side» of the «weak» in terms of knowledge exchange element).

Parameters of the edge lying between the vertices with the numbers 2 and 5 are defined as indicators of disjunctive strength for routes passing through this element. Substantially, this connection means а reliable knowledge dissemination channel, both in terms of time for distribution, and from the point of view of professional interests matching: individuals communicate frequently and use «the same language».

For each pair of connected vertices we calculated the cumulative strength of the routes, which are the elements of the fuzzy reachability matrix in cognitive and time units $(\tilde{D}_{n\times n}^{\alpha})$ and $\tilde{D}_{n\times n}^{\beta}$. These indicators allow a comprehensive analysis of the conductivity of knowledge within the network based on two parameters that determine the quality of the dissemination of knowledge. Tab. 4 contains the results of calculations of cumulative strengths routes in the network in question.

Table 4

v _i	v _i	v_1	<i>v</i> ₂	<i>v</i> ₃	<i>v</i> ₄	<i>v</i> ₅	<i>v</i> ₆	v_7	v_8	<i>v</i> 9	<i>v</i> ₁₀	<i>v</i> ₁₁	<i>v</i> ₁₂	<i>v</i> ₁₃	<i>v</i> ₁₄	<i>v</i> ¹⁵
<i>v</i> ₁	α		0.58	0	0	0.58	0.52	0.38	0	0.52	0.67	0.17	0	0	0.11	0
	β		0.29	0.31	0.05	0.31	0.18	0.31	0.19	0.18	0.31	0.05	0.01	0.01	0.01	0.01
<i>v</i> ₂	α	0.58		0	0	0.75	0.89	0.4	0	0.89	0.65	0.18	0	0	0.11	0
	β	0.29		0.93	0.14	0.93	0.62	0.93	0.58	0.62	0.93	0.14	0.02	0.02	0.02	0.02
<i>v</i> ₃	α	0	0		0	0	0	0	0	0	0	0	0	0	0	0
	β	0.31	0.93		0.16	1	0.58	1	0.62	0.58	1	0.16	0.02	0.02	0.02	0.02
<i>v</i> ₄	α	0	0	0		0	0	0	0	0	0	0	0.2	0.45	0	0.12
	β	0.05	0.14	0.16		0.16	0.09	0.16	0.1	0.09	0.16	0.02	0.16	0.16	0.004	0.16
<i>v</i> ₅	α	0.58	0.75	0	0		0.67	0.5	0	0.67	0.87	0.22	0	0	0.14	0
	β	0.31	0.93	1	0.16		0.58	1	0.62	0.58	1	0.16	0.02	0.02	0.2	0.02
v ₆	α	0.52	0.89	0	0	0.67		0.45	0	1	0.58	0.2	0	0	0.13	0
	β	0.18	0.62	0.58	0.09	0.58		0.58	0.36	1	0.58	0.09	0.01	0.01	0.01	0.01
<i>v</i> ₇	α	0.38	0.4	0	0	0.5	0.45		0	0.45	0.58	0.45	0	0	0.28	0
	β	0.31	0.93	1	0.16	1	0.58		0.62	0.58	1	0.16	0.02	0.02	0.02	0.02
<i>v</i> ₈	α	0	0	0	0	0	0	0		0	0	0	0	0	0	0
	β	0.19	0.58	0.62	0.1	0.62	0.36	0.62		0.36	0.62	0.1	0.01	0.01	0.01	0.01
<i>v</i> ₉	α	0.52	0.89	0	0	0.67	1	0.45	0		0.58	0.2	0	0	0.13	0
	β	0.18	0.62	0.58	0.09	0.58	1	0.58	0.36		0.58	0.09	0.01	0.01	0.01	0.01
<i>v</i> ₁₀	α	0.67	0.65	0	0	0.87	0.58	0.58	0	0.58		0.26	0	0	0.16	0
	β	0.31	0.93	1	0.16	1	0.58	1	0.62	0.58		0.16	0.02	0.02	0.02	0.02
<i>v</i> ₁₁	α	0.17	0.18	0	0	0.22	0.2	0.45	0	0.2	0.26		0	0	0.63	0
	β	0.05	0.14	0.16	0.02	0.16	0.09	0.16	0.1	0.09	0.16		0	0	0.16	0
<i>v</i> ₁₂	α	0	0	0	0.2	0	0	0	0	0	0	0		0.45	0	0.58
	β	0.01	0.02	0.02	0.16	0.02	0.01	0.02	0.01	0.01	0.02	0		1	0	1
<i>v</i> ₁₃	α	0	0	0	0.45	0	0	0	0	0	0	0	0.45		0	0.26
	β	0.01	0.02	0.02	0.16	0.02	0.01	0.02	0.01	0.01	0.02	0.004	1		0	1
<i>v</i> ₁₄	α	0.11	0.11	0	0	0.14	0.13	0.28	0	0.13	0.16	0.63	0	0		0
	β	0.01	0.02	0.02	0.004	0.02	0.01	0.02	0.01	0.01	0.02	0.16	0.0006	0		0
<i>v</i> ₁₅	α	0	0	0	0.12	0	0	0	0	0	0	0	0.56	0.26	0	
	β	0.01	0.02	0.02	0.16	0.02	0.01	0.02	0.01	0.01	0.02	0	1	1	0	

The cumulative strength of routes between the vertexes in time and cognitive units



Fig. 3. Connected components in the parametrized network

At this phase of the knowledge conductivity analysis we can make a preliminary conclusion about the strength of the routes of the entire network. As seen from the table above, only a few routes have strengths exceeding the threshold $\alpha = 0.5$ and $\beta = 0.5$ (highlighted in color). There are only ten such routes of forty-two possible. Even now we can conclude uneven coverage of the network by «working» («strong») contacts, which makes the process of knowledge transfer chaotic and unorganized in the network in its current configuration.

On the basis of the cumulative strengths the model determines connected components that stand for groups of employees, in which there is the most intensive exchange of knowledge and competencies. In the example we settled the threshold levels of knowledge sharing to following values: $\alpha = 0.7$ and $\beta = 0.9$. The following connected components appeared as a result of calculation: (v_2, v_5, v_{10}) and (v_6, v_9) . Fig. 3 illustrates the results obtained.

The final stage of the analysis involves consideration of the general knowledge conductivity characteristics of the network. The developed model indicators help to assess the current state of the network and make a comparative analysis after application of reorganization measures, directly or indirectly affecting the throughput performance of the network.

For a comparative analysis different states of the network, in the example of we have simulated management actions to reorganize the connections in the network in order to improve the conductivity of knowledge between employees. Based on the analysis of cognitive potential parameters of knowledge sharing between employees in the network we have partially established new contacts between those pairs of individuals for which the rate of cognitive potential of knowledge sharing exceeds 0.9. In fact, new edges were added to the initial graph (by indexes of the vertexes): 1 - 9, 1 - 6, 2 - 11, 2 - 13, 2 - 1315, 5 - 6, 6 - 10, 6 - 11, 9 - 10, 9 - 11, 11 -13, 11 - 15, 13 - 15, 14 - 15. For each of the added links indicator of the intensity of communication was established at 0.9 (in practice it may be achieved by introducing regular round tables for the staff). Fig. 4 illustrates a new connection in the network (the values for the parameters are set only for «new» edges).

Tab. 5 contains the results of calculations of the knowledge conductivity main characteristics for both cases - the initial state and after the implementation of new connections between the employees.

As the table shows, the average strength indicators have improved markedly after the new routes determination between some pairs of employees. This gives grounds to conclude that the updated network communication channels between employees more reliable and stable. This in its turn makes it possible to assume that in the new network, there is an intense circulation of knowledge with greater reliability and, as a result, efficiency. An additional argument in favor of this



Fig. 4. Reorganized network of knowledge dissemination

Table 5

Parameters of knowledge conductivity in the network for the initial state and after the reorganization of the network

Parameter	Initial network	After the reorganization
Average strength of the route in terms of cognitive units	0.23	0.5
Average strength of the route in terms of time units	0.32	0.75
The amount of interests group	2	1
The average number of interest groups (connected components)	2.5	10

conclusion is the indicators of the amount of interest groups and their average number. As soon as the model example considers one area of knowledge common to the entire group of 15 people, it is logically reasonable to assume that if there is a particularly cohesive internal team of ten people, in which there is active and productive

communication, knowledge will be intensively and effectively spread between the employees. In the reverse situation, when interest groups numerically small (2, 3 persons) and relatively few in the whole team, as shown in the example before the reorganization of relations, knowledge spreading will take a relatively long time and the knowledge itself will remain virtually inaccessible to other members of the team.

The provided example helps to evaluate the application and use of the model and to identify possible directions for its further development. Thus, for any enterprise in which the main production resource is knowledge, the model provides an opportunity to assess how the organization has established communication between its employees and how these relationships contribute to the spread of knowledge. The model uses qualitative characteristics of the diffusion of knowledge, which is an adequate reflection of the properties of such a complex and difficult process, as the dissemination of knowledge.

Conclusion. Scientific discoveries and innovations usually accumulate practices of several generations researchers. of scientists and Knowledge in this or the other area, reaching a certain critical mass, embodies in a new knowledge and moves to a new form. The ability to implement existing and newly created knowledge into economic products and operate knowledge as a product of modern economy is considered to be the key to success for organizations of different structures and sizes - from start-ups to international corporations and enterprises.

Nowadays, these facts are recognized at all levels of administrative management, in both the public and private sector.

As a result, analysis and development of applied tools for assessing and modeling processes of knowledge dissemination is an urgent scientific problem. The concept of numbers at all times has been the basis of decision-making.

Within the framework of this article the authors present a model, developed for the

REFERENCES

1. The Global Innovation Index 2014 .: ratings lead Switzerland, the United Kingdom and Sweden for positive changes in Africa south of the Sahara; human factor - the driving force of innovation. URL: http://www.wipo.int/pressroom/ru/articles/2014/article_ 0010.html (accused March 03, 2015). (rus)

2. Mindeli L.E. Conceptual aspects of the formation of the knowledge economy. Problems of Forecasting, 2007, no. 3, pp. 115-136. (rus)

3. Milner B.Z. The concept of knowledge management in modern organizations. Russian Management Journal, 2003, no. 1, pp. 57-76. (rus)

4. Karlik A.Ye., Platonov V.V., Tikhomirov N.N., Vorob'yev V.P., Kovaleva A.S. Management of intellectual resources of innovation active enterprises. St. Petersburg, SPbGEU, 2013. 167 p. (rus)

5. Silkina G.Iu., Shevchenko S.Iu. Innovation processes in the knowledge economy. Analysis and modeling. St. Petersburg, Publishing House of the Polytechnic University, 2014. 167 p. (rus)

6. Ratner S.V. Scripts of stratification of scientific innovation networks. Managing large systems. Special edition «Network management model, 2010, no. 30-1, pp. 774-798. (rus)

7. Bakanova S.A. Graph-analytical model of knowledge spreadng in organizations. St. Petersburg State Polytechnical University Journal. Economics, 2015, no. 1(211), pp. 189-196 (rus).

8. Cowan R., Jonard N. Network Structure and the Diffusionof Knowledge. Journal of Economic Dynamics and Control, 2004, vol. 8, no. 28, pp. 1557-1575.

9. Gubanov D.A., Novikov D.A., Chkhartishvili A.G.

analysis and evaluation of the knowledge dissemination process. The model can be used to support management decisions in important emerging stream of Management - Knowledge Management. Corporate social networks, which contain information about the knowledge and competencies of the employees and support electronic forms of communication, can serve as an information base for using the model in real companies. The authors see the following necessary directions for further research of this model.

- the introduction of fuzzy characteristics for describing the structure of the employees knowledge - this will bring a possibility to construct more precise assessment of staff knowledge and cognitive capacity among them;

- introduction of a time-dependent factor of knowledge assimilation by the individuals – this will allow to define the time characteristics of knowledge dissemination process, to consider dynamics of knowledge accumulation.

Models of influence in social networks. Managing large systems, 2009, no. 27, pp. 205-281. (rus)

10. Bershteyn L.S., Bozhenyuk A.V. Fuzzy graphs and hypergraphs. Moscow, Scientific World, 2005. 256 p. (rus)

11. Tuzovskiy A.F., Chirikov S.V., Yampol'skiy V.Z. Knowledge management systems (methods and technologies). Ed. V.Z. Yampolsky. Tomsk, Publishing House of the YTL, 2005. 260 p. (rus)

12. Babkin A.V., Khvatova T.Iu. The influence of the institutional environment for the development of the national innovation system. Russian Scientific Journal of Economics and Management, 2011, no. 6(68), pp. 64-73. (rus)

13. Glukhov V.V., Korobko S.B., Marinina T.V. Knowledge Economy: Textbook. St. Petersburg, Peter, 2003. 528 p. (rus)

14. Stepanova T.Ye., Manokhina N.V. Economy based on knowledge (theory and practice): a tutorial. Moscow, Gardariki, 2008. 238 p. (rus)

15. Nonaka I., Takeuchi Kh. Company - creator of knowledge. Origin and development of innovation in Japanese firms. Moscow, Olympus -Business, 2011. 384 p. (rus)

16. Silkina G.Iu., Shevchenko S.Iu. Models of knowledge exchange. St. Petersburg State Polytechnical University Journal. Economics, 2012, no. 2-1(211), pp. 125-131 (rus).

17. Makarov V.L. Overview of the economic models of the economy with innovation. Economics and Mathematical Methods, 2009, vol. 45, no. 1, pp. 3-14. (rus)

СПИСОК ЛИТЕРАТУРЫ

1. Глобальный инновационный индекс 2014 г.: в рейтингах лидируют Швейцария, Соединенное Королевство и Швеция при положительных изменениях в странах Африки к югу от Сахары; человеческий фактор — движущая сила инноваций. URL: http://www.wipo.int/pressroom/ru/articles/2014/article_ 0010.html (дата обращения: 03.03.2015).

2. Миндели Л.Э. Концептуальные аспекты формирования экономики знаний // Проблемы прогнозирования. 2007. № 3. С. 115–136.

3. **Мильнер Б.З.** Концепция управления знаниями в современных организациях // Российский журнал менеджмента. 2003. № 1. С. 57–76.

4. Карлик А.Е., Платонов В.В., Тихомиров Н.Н., Воробьев В.П., Ковалева А.С. Управление интеллектуальными ресурсами инновационно-активных предприятий. СПб.: Изд-во СПбГЭУ, 2013. 167 с.

5. Силкина Г.Ю., Шевченко С.Ю. Инновационные процессы в экономике знаний. Анализ и моделирование. СПб.: Изд-во Политехн. ун-та, 2014. 167 с.

6. Ратнер С.В. Сценарии стратификации научно-инновационной сети // Управление большими системами. Спец. вып. «Сетевые модели управления». 2010. № 30-1. С. 774–798

7. Баканова С.А. Графоаналитическая модель распространения знаний в организациях // Научно-технические ведомости Санкт-Петербургского государственного политехнического университета. Экономические науки. 2015. № 1(211). С. 189–196.

8. Cowan R., Jonard N. Network Structure and the Diffusionof Knowledge // Journal of Economic Dynamics

and Control, 2004, vol. 8, no. 28, pp. 1557-1575.

9. Губанов Д.А., Новиков Д.А., Чхартишвили А.Г. Модели влияния в социальных сетях // Управление большими системами. 2009. № 27. С. 205–281.

10. Берштейн Л.С., Боженюк А.В. Нечеткие графы и гиперграфы. М.: Научный мир, 2005. 256 с.

11. Тузовский А.Ф., Чириков С.В., Ямпольский В.З. Системы управления знаниями (методы и технологии) / под общ. ред. В.З. Ямпольского. Томск: Изд-во НТЛ, 2005. 260 с.

12. Бабкин А.В., Хватова Т.Ю. Влияние институциональной среды на развитие национальной инновационной системы // Российский научный журнал Экономика и управление. 2011. № 6(68). С. 64–73.

13. Глухов В.В., Коробко С.Б., Маринина Т.В. Экономика знаний: учеб. пособие. СПб.: Питер, 2003. 528 с.

14. Степанова Т.Е., Манохина Н.В. Экономика, основанная на знаниях (теория и практика): учеб. пособие. М.: Гардарики, 2008. 238 с.

15. Нонака И., Такеучи Х. Компания – создатель знания. Зарождение и развитие инноваций в японских фирмах. М.: Олимп-Бизнес, 2011. 384 с.

16. Силкина Г.Ю., Шевченко С.Ю. Модели обмена знаниями // Научно-технические ведомости Санкт-Петербургского государственного политехнического университета. Экономические науки. 2012. № 2-1(144). С. 125-131.

17. Макаров В.Л. Обзор экономических моделей экономики с инновациями // Экономика и математические методы. 2009. Т. 45, № 1. С. 3–14.

BAKANOVA Svetlana A. – Peter the Great St. Petersburg Polytechnic University. 195251. Politechnicheskaya str. 29. St. Petersburg. Russia. E-mail: sveta.bakanova89@gmail.com

БАКАНОВА Светлана Александровна – аспирант Санкт-Петербургского политехнического университета Петра Великого.

195251, ул. Политехническая, д. 29, Санкт-Петербург, Россия. E-mail: sveta.bakanova89@gmail.com

SILKINA Galina Iu. – Peter the Great St. Petersburg Polytechnic University.

195251, ул. Политехническая, д. 29, Санкт-Петербург, Россия. E-mail: galina.silkina@gmail.com

СИЛКИНА Галина Юрьевна – профессор Санкт-Петербургского политехнического университета Петра Великого, доктор экономических наук.

195251, ул. Политехническая, д. 29, Санкт-Петербург, Россия. E-mail: galina.silkina@gmail.com